

COURS_5 : LE PLUS COURT CHEMIN DANS UN GRAPHE 2

I. Algorithme de Dijkstra avec FILE :

Algorithme de Dijkstra :

```
dist[∞ for u in G]
P[-1 for u in G]
s = 0
Q = []
Q.append(s)
dist[s] = 0

while Q :
    z = delete()
    for x in adj[z] :
        tense = d[z] + W[z][x]
        if dist[x] > tense :
            dist[x] = tense
            P[x] = z
            Q.add(x)
```

Algorithme de Dijkstra :

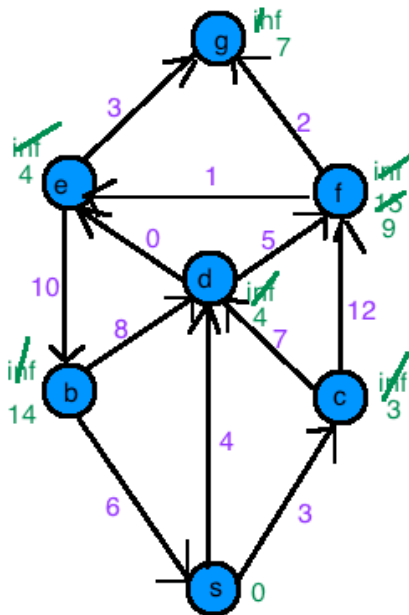
```
dist[∞ for u in G]
P[-1 for u in G]

Q = V
dist[s] = 0
P[s] = s

while Q :
    z = Q.deleteMin()
    for x in adj[z] :
        tense = d[z] + W[z][x]
        if dist[x] > tense :
            dist[x] = tense
            P[x] = z
```

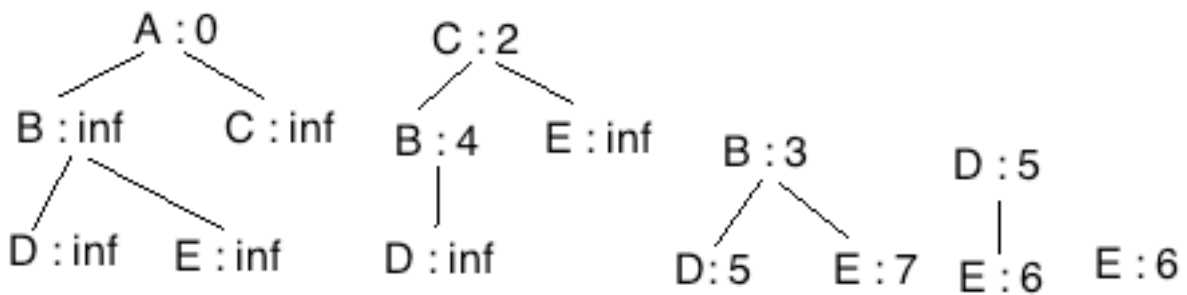
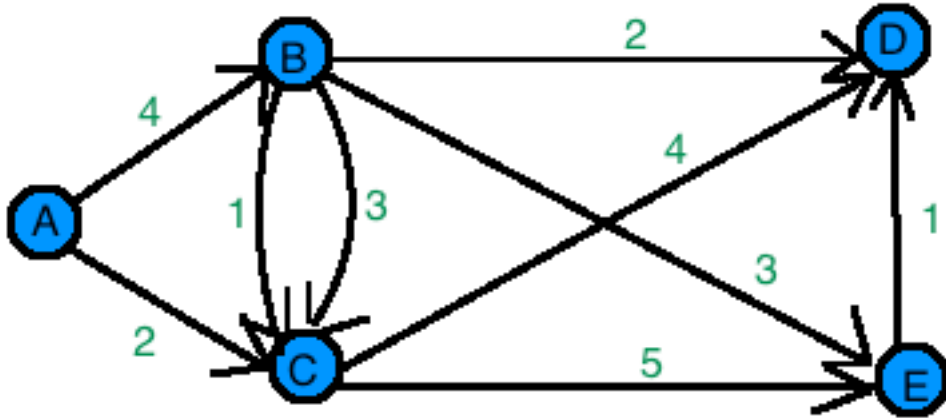
=> $O(V^2 + E)$

exemple :



Problème : a chaque fois on cherche le min pour le supprimer c'est pourquoi la complexité est aussi grande.

II. Algorithme de Dijkstra avec TAS :

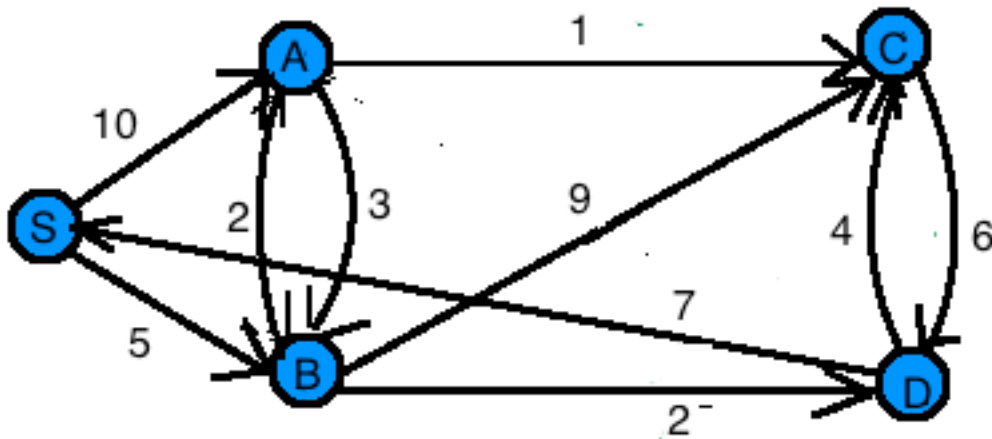


III. Module heapp sur python : (heap = tas en anglais)

```
heappop(Q)
heappush(Q,x)
heapify(Q)
heapreplace(Q)
```

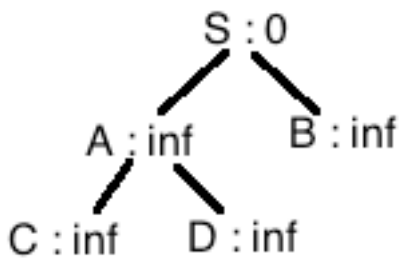
IV. Exercice :

faire le parcours du graphe suivant :

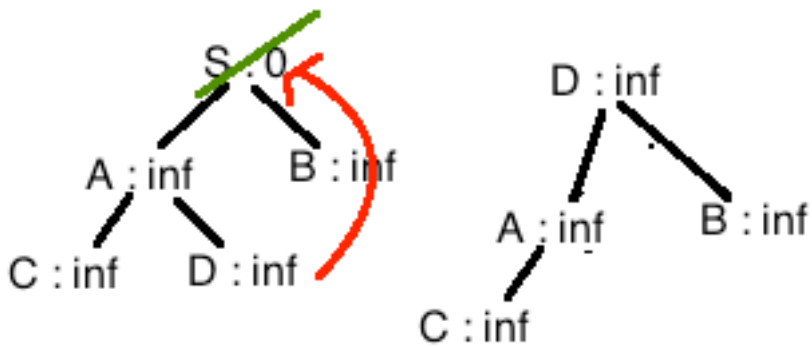


1. si $Q = V$
2. si $Q = \{s\}$

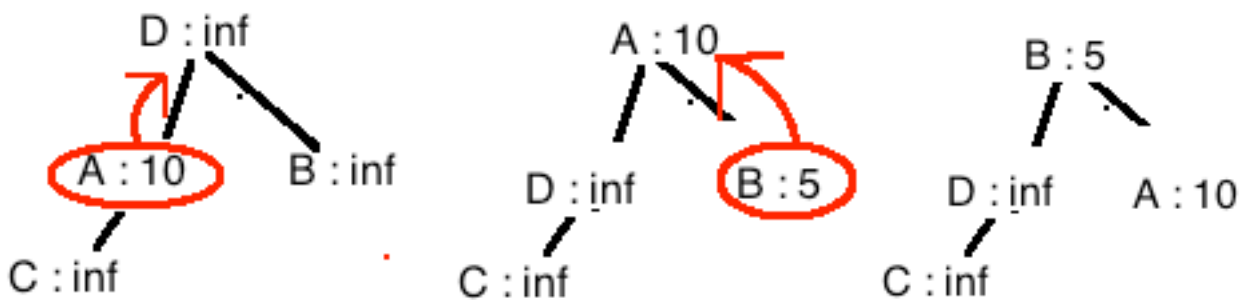
1.

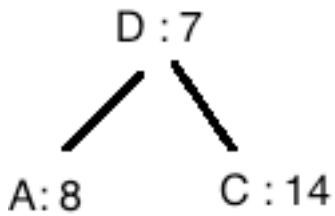
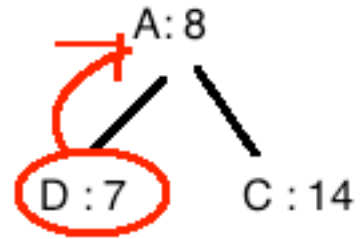
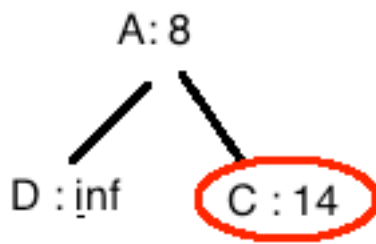
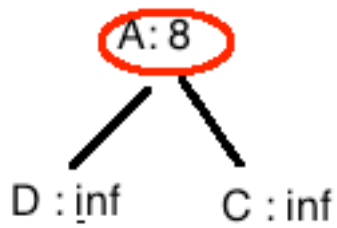
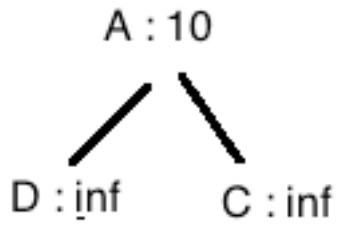
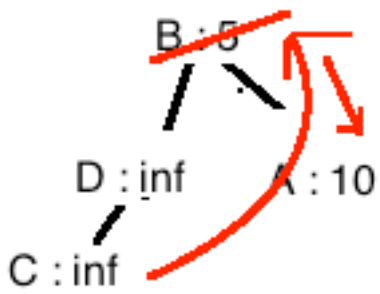


1. On supprime S

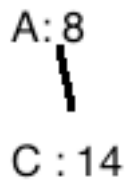
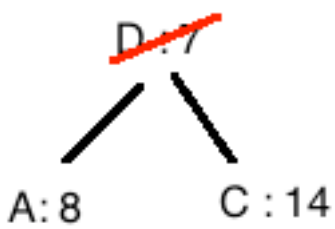


On modifie

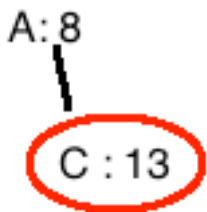




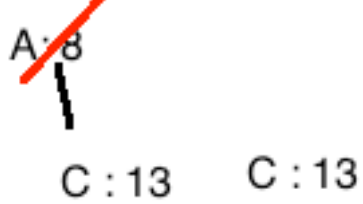
On supprime D



on modifie



On supprime A



on modifie

C : 9

on supprime C

~~C : 9~~

TAS VIDE -> FIN !!!

2. SI Q = {S}

S : 0 ~~S : 0~~

